

Application Note :

## Measuring Polarization Dependant Frequency in DPSK Demodulator

### 1. General Description

The polarization dependant frequency (PDF) of an interferometer is the maximum shift in frequency at a given phase at every polarization.

### 2. Measurements

The Stokes measurement<sup>[1]</sup> are performed using the 4 polarizations: linear horizontal, vertical, diagonal and circular right hand. Post-processing these transmission data provide PDL and PDF.

### 3. Post-Processing Data

The transmission of the demodulator is expressed as follow:

$$Q_j(\nu) = \left[ \frac{T_j(\nu)}{2} \times \left\{ 1 + \sin \left( 2\pi \frac{\nu}{FSR} + \varphi_j(\nu) \right) \right\} + \varepsilon_j(\nu) \right]$$

Where:

- $j$  (= 1 to 4) represents the polarization state as defined in Stokes measurements;
- $Q$  is the transmission of the device under test;
- $\nu$  is the frequency ;
- $T$  is the amplitude of the sine function (interferometer modulation);
- $FSR$  is the free spectral range of the interferometer. It is independent on polarization and wavelength, at least an order of magnitude below requirements for PDF measurement;
- $\varphi$  is a reference phase that can change with polarization. It will be referred to as “null frequency phase”;
- $\varepsilon$  is the remaining transmission when the interferometer is on a destructive interference frequency (it roughly is the interferometer isolation).

A sinus fitting algorithm is applied to the 4 transmissions to retrieve the experimental values of the above equation. One can show that taking exactly the same procedure as in [1], it is possible to express the maximum and minimum of the null-frequency phase over every polarization. Therefore, the PDF can be expressed from this analysis and takes the following form:

$$PDF \approx \frac{\sqrt{\left(\frac{\varphi_1 - \varphi_2}{2}\right)^2 + \left(\varphi_3 - \frac{\varphi_1 + \varphi_2}{2}\right)^2 + \left(\varphi_4 - \frac{\varphi_1 + \varphi_2}{2}\right)^2}}{\pi} FSR$$

The detailed mathematics about the technique will be presented [2].

One can see that it is more relevant to express PDF as a shift normalized in frequency since it scales with FSR. Therefore, we recommend referring to PDF as a fraction of the FSR instead of absolute value in Hz.

#### 4. References

1. Hentschel C., Schmidt S., *Polarization Measurements using the Agilent 8169A Polarization Controller*. Product note available on Agilent's website.  
[http://www.home.agilent.com/agilent/redirector.jsp?action=ref&cname=AGILENT\\_EDITORIAL&cc=US&lc=eng&ckey=115278&nid=-35518.536883082&pid=72344](http://www.home.agilent.com/agilent/redirector.jsp?action=ref&cname=AGILENT_EDITORIAL&cc=US&lc=eng&ckey=115278&nid=-35518.536883082&pid=72344)
2. Max J.-J., O'Reilly S. *From Stokes measurements to PDF post-processing*. White paper available on ITF Labs website